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A heuristic to minimize the cardinality of a real-time task set by automated task clustering

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Abstract

We propose in this paper a method to automatically map functionalities (blocks of code corresponding to high-level features) with real-time constraints to tasks (or threads). We aim at reducing the number of tasks functions are mapped to, while preserving the schedulability of the initial system. We consider independent tasks running on a single processor. Our approach has been applied with fixed-task or fixed-job priorities assigned in a Deadline Monotonic (DM) or a Earliest Deadline First (EDF) manner.

1 Introduction

Our work falls within the scope of real-time systems programming. Usually, real-time system developers design a system as a set of functionalities with real-time constraints. A functionality is here considered a block of code corresponding to a high-level feature. Implementing such systems requires to map each functionality to a real-time task (thread). On the one hand, the number of those functionalities is quite high. For instance, it ranges from 500 to 1000 in the flight control system of an aircraft or of a space vehicle [7, 11]. On the other hand, a large number of threads implies a significant time overhead in context switching [27, 15] and an important memory footprint (e.g. task control block, size of the stack, etc.). Thus, the number of tasks supported by embedded real-time operating systems is limited, rarely over one hundred, and developers cannot map each functionality to a different

task. This mapping is currently mainly performed manually and, given the number of functionalities to process, this work can be tedious and error-prone.

In our work, we address this question from the scheduling point of view. We model a system as a set of tasks with real-time constraints, where each task is characterized by an execution time, an activation period and a deadline, in the same way as Liu and Layland’s task model [18]. With respect to this model, functionalities can simply be considered as finer grain tasks, while threads are just coarser tasks. Thus, mapping functionalities to tasks amounts to gathering several tasks into a single one, which we call *task clustering*. Clustering several tasks implies to choose only one deadline for the cluster, which effectively reduces some task deadlines. As a consequence, we have to check that the system schedulability is preserved after the clustering.

Related Work In the literature, task clustering is most often studied in the context of distributed systems implementation, where it consists in distributing a set of tasks over a set of computing nodes (processors or cores). This is different from our context, because in the distributed systems context a cluster corresponds to the set of tasks allocated to the same computing resource. For instance, [23, 1] aim at minimizing communications by clustering tasks that communicate a lot. The approaches in [22, 13] cluster tasks based on communications, in order to reduce the system makespan. The number of tasks of the resulting implementation is however not reduced.

Functionality to task mapping is known as runnable-to-task mapping and is identified as a step of the de-

velopment process in the augmented real-time specification for AUTomotive Open System ARchitecture (AUTOSAR) [5]. This document and [27] also provide guidelines defining under which conditions runnables can be mapped to the same tasks. Authors in [32] propose an automated mapping in that context, but that work is restricted to functionalities that have deadlines equal to their periods. In [8, 21], the authors study the multi-task implementation of multi-periodic synchronous programs and must allocate the different elements of the program to tasks. The clustering is out of the scope of [21], while the heuristic proposed in [8] is very specific to the language structure.

In [26], authors aim at reducing the number of tasks in order to reduce the complexity of the scheduling problem. However, they only focus on functional requirements to group tasks, without considering timing constraints.

This research Our objective is to automate the task clustering, so as to reach a minimal task number, while preserving the system schedulability. The number of possible clusterings of a task set is equal to the number of partitions of the set, which is in the range of the *Bell number* [24]. The Bell number is exponential with respect to the cardinality of the set, so given the huge number of possibilities to explore, we use a greedy heuristic to search the partitions space. For now, we do not consider communications and the execution platform is made up of a single processor. These are strong restrictions, which will be lifted in future work. The aim of the paper is to properly define the problem and to study it in a simple setting, so as to serve as a basis for future work.

Organization The rest of the paper is organized as follows. In Section 2, we describe our clustering model. Section 3 is dedicated to the verification of cluster schedulability. We describe the way we generate solutions and the heuristic applied in Section 4. Section 5 contains the experimental results conducted on large sets of tasks, randomly generated. Finally, we expose our conclusion and the future work involved in the Section 6.

2 Problem definition

Our model, illustrated in Figure 1, is based on Liu and Layland's model [18]. A system consists of a synchronous (i.e. with offsets equal to zero) set of real-time tasks $\mathcal{S} = (\{\tau_i(C_i, D_i, T_i)\}_{1 \leq i \leq n})$ where C_i is the worst-case execution time (WCET) of τ_i , T_i is the activation period, D_i is the relative deadline with $D_i \leq T_i$. We denote $\tau_{i,k}$ the $(k+1)^{th}$ ($k \geq 0$) instance, or *job*, of τ_i . The job $\tau_{i,k}$ is released at time $o_{i,k} = kT_i$. Every job $\tau_{i,k}$ must be completed before its absolute deadline $d_{i,k} = o_{i,k} + D_i$

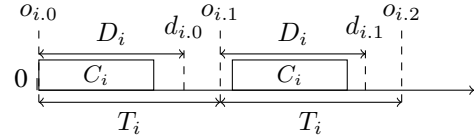


Figure 1: Task Diagram.

2.1 Scheduling

In this paper, we focus on priority-based scheduling policies, either fixed-job with Earliest Deadline First (EDF) [18] or fixed-task priority policies with Deadline Monotonic (DM) [16].

Let \mathcal{J} denote the infinite set of job $\mathcal{J} = \{\tau_{i,k}, 1 \leq i \leq n, k \in \mathbb{N}\}$. Given a priority assignment Φ , we define two functions $s_\Phi, e_\Phi : \mathcal{J} \rightarrow \mathbb{N}$, where $s_\Phi(\tau_{i,k})$ is the start time and $e_\Phi(\tau_{i,k})$ is the completion time of $\tau_{i,k}$ in the schedule produced by Φ .

Definition 1. Let $\mathcal{S} = (\{\tau_i\}_{1 \leq i \leq n})$ be a task set and Φ be a priority assignment. \mathcal{S} is schedulable under Φ if and only if: $\forall \tau_{i,k}, e_\Phi(\tau_{i,k}) \leq d_{i,k} \wedge s_\Phi(\tau_{i,k}) \geq o_{i,k}$

In the sequel, we will also rely on the notion of *laxity*.

Definition 2. Laxity L (or slack time) indicates the maximum delay that can be taken by the task without exceeding its deadline: $L_i = D_i - C_i$.

2.2 Clustering

Definition 3. Clustering τ_i and τ_j , where $D_i \leq D_j$, produces a cluster τ_{ij} with the following parameters:

$$C_{ij} = C_i + C_j$$

$$T_{ij} = T_i = T_j$$

$$D_{ij} = D_i$$

The cluster deadline is the shortest of the two tasks. Taking the minimum deadline ensures we respect both initial deadlines, even though the constraints will be, in general, more stringent than the initial constraints. By definition, we only group tasks with identical periods.

Definition 4. Let $\mathcal{S} = (\{\tau_i\}_{1 \leq i \leq n})$ be a task set and τ_x and τ_y be two tasks of \mathcal{S} such that $D_x \leq D_y$. We say that τ_{xy} is a valid cluster if and only if:

1. $L_x \geq C_y$
2. The task set obtained after clustering is schedulable

In industrial practices, functionalities of different periods are sometimes mapped together, especially when these functionalities interact a lot, to minimize communication as explained in [28]. This possibility makes the clustering more complex because it requires to manage scheduling inside a cluster. For this reason, we do not deal with this option in this paper. Nevertheless, we could relax this assumption via, e.g., hierarchical scheduling [17].

The laxity test is just an optimization. It is redundant with the schedulability test but it is simpler to check (constant time). Laxity is depicted in Subfigure 2(a).

A schedulable system might become non schedulable after clustering, as illustrated in Figure 2. Indeed, we notice in Subfigure 2(b) that the task τ_b misses its first deadline after the clustering of tasks τ_a and τ_c . Thus, we must check the resulting task set schedulability after clustering.

3 Checking cluster schedulability

Conditions 1 of the Definition 4 can be checked trivially in constant time. Nevertheless, condition 2 is more complex. Indeed, as we intend to check schedulability of a large number of solutions (i.e. at each step of the clustering process), considering a suitable schedulability test is important.

A schedulability test is called sufficient if all task sets considered schedulable by the test are actually schedulable. In the same manner, a schedulability test is called

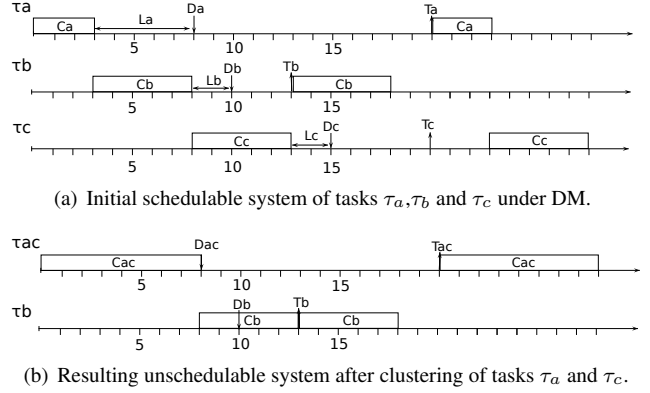


Figure 2: Influence of task clustering on system schedulability.

necessary if all task sets considered unschedulable by the test are in fact unschedulable. Schedulability tests that are both sufficient and necessary are referred to as exact.

In this section, we review existing schedulability tests that can be used for clustering under DM and EDF scheduling policies. We only consider exact or sufficient tests insuring that the task sets obtained after clustering are schedulable. Indeed, applying sufficient tests means that we might not get the minimum number of clusters but we are sure to obtain a valid clustering. Notice that we work with synchronous (with offsets equal to zero) task sets that have constrained deadlines (i.e. with $D_i \leq T_i$).

3.1 Exact schedulability tests

Authors in [9] distinguish two types of tests: *Boolean schedulability tests* and *response time tests*. On the one hand, Boolean tests give a Boolean answer, determining only whether a task set is schedulable or not, for instance with processor demand analysis (PDA) as the Quick convergence Processor-demand Analysis (QPA) [31]. On the other hand, exact tests based on response time analysis (RTA) provide worst response time for each task. The response time of a task is the time elapsed between its release and the time when it finishes its job.

Deadline Monotonic RTA [14, 3] of a task τ_i is based on the concept of level- i busy period. The level- i busy period is the maximum continuous time interval during

which a processor executes tasks of higher or equal priority to the priority of the considered task τ_i , until τ_i finishes its active job. Then, the computation of the worst response time for each task τ_i is based on the length of level- i busy period. RTA for DM can be performed with a pseudo-polynomial time algorithm.

Earliest Deadline First Contrary to fixed-task priority (FP) systems, the worst response time is not necessarily found on the first processor busy period in a task set scheduled by EDF [30]. Thus, computing RTA for EDF is more complex and has an exponential complexity.

3.2 Sufficient schedulability conditions

In order to reduce the complexity of the computations, we also considered linear sufficient schedulability tests. Audsley [4] and Devi [10] propose sufficient but not necessary schedulability tests, respectively for DM and EDF in $\mathcal{O}(n)$ complexity. As far as we know, there are no more efficient tests for DM and EDF in linear complexity. The first results show that the test for DM behaves well for clustering and better than that of EDF. Those two sufficient tests actually provide an approximate worst response time for each task. They can be considered an approximate RTA analysis.

4 Minimizing the number of tasks

In this section, we detail our approach for minimizing the size of the initial task set by successive clusterings. Due to size of the search space, we rely on a heuristic instead of an exact algorithm.

4.1 Search space

Our problem consists in finding a partition of the task set that is schedulable and with a minimum number of subsets. A partition of a set \mathcal{X} is a set of nonempty subsets of \mathcal{X} such that every element n in \mathcal{X} is in exactly one of these subsets. The number of partitions of a set is the Bell number [24]. The Bell number is exponential with respect to the size of \mathcal{X} and can be computed by the following recurrence relation:

$$B_{n+1} = \sum_{k=0}^n \binom{n}{k} B_k \text{ with } B_0 = 1$$

As we only cluster tasks with identical periods, the search space can be restricted to $\prod_{i=0}^m B_{n_i}$ where B_{n_i} is the Bell number of set i of n tasks with equal periods and m is the number of sets. Nevertheless, this number remains exponential. To give a better idea of the size of the search, notice that for instance, $B_{500} \simeq 10^{844}$.

4.2 Partitions enumeration

A naive solution might be to conduct an exhaustive search among all partitions of the initial task set, e.g. by applying partitions generation algorithms [2, 20]. Nonetheless, our first experimentations show that, even using sufficient linear tests, this solution is not achievable due to the exponential number of partitions to explore. For instance, experiments conducted on a 2.3GHz Intel Core i7 quad-core with 4GByte memory, from an initial set of 20 tasks, lead to more than several days of computation. Thus, we think that it is necessary to limit the search space by applying a heuristic.

Our technique is derived from a simple recursive method found in Section 17.1 of [2]. For instance, for the set $\{\{A\}, \{B\}, \{C\}\}$ we generate the following 3 partitions in a first step:

$$\begin{aligned} &\{\{A\}, \{B, C\}\} \\ &\{\{A, C\}, \{B\}\} \\ &\{\{A, B\}, \{C\}\} \end{aligned}$$

We apply recursively this principle for each partition generated until we obtain a partition with a unique element. This situation corresponds to having all tasks regrouped in a single cluster. This enumeration produces a tree as illustrated in Figure 3. Notice that this recursive algorithm generates many duplicates. For example, we can observe in the Figure 3 that the partition $\{\{A\}, \{B, C, D\}\}$ appears twice. However, our heuristic always selects a single child by recursive call so we do not encounter duplicates.

sponds to the sum of the first n triangular numbers (also called tetrahedral numbers) and its closed-form expression is $f(n) = \frac{n(n+1)(n+2)}{6}$ [29]. Hence, this sequence complexity is $\mathcal{O}(n^3)$. We apply a sufficient schedulability test in $\mathcal{O}(n)$ complexity (whether with DM or EDF) on each visited partition, so the heuristic complexity is $\mathcal{O}(n^3) \times \mathcal{O}(n) = \mathcal{O}(n^4)$. In a similar way, applying schedulability tests with a pseudo-polynomial complexity gives a pseudo-polynomial complexity to the whole algorithm. \square

Algorithm 1 Automated task clustering algorithm

Function clustering(S)

Require: $\mathcal{S} = (\{\tau_i\}_{1 \leq i \leq n})$: initial set of tasks in ascending deadline order

```

minSumTests  $\leftarrow n + 1$ 
minSet  $\leftarrow null$ 
for  $i = n - 1$  to  $0$  do //find the best child
    for  $j = i - 1$  to  $0$  do
        if  $T_i == T_j$  then
            if  $C_i + C_j \leq \min(D_i, D_j)$  then //laxity
                 $S' \leftarrow \{S \setminus \{\tau_i, \tau_j\}\} \cup \tau_{ij}$ 
                if schedulable( $S'$ ) then
                    if  $h(S) < \minSumTests$  then
                         $\minSumTests \leftarrow h(S)$ 
                         $\minSet \leftarrow S'$ 
                    end if
                end if
            end if
        end if
    end for
end for

if  $\minSet \neq null$  then
    return clustering( $\minSet$ ) //continue with best child
else
    return  $S$ 
end if

```

5 Experimental results

5.1 Task set generation

We chose the following model to generate random task sets:

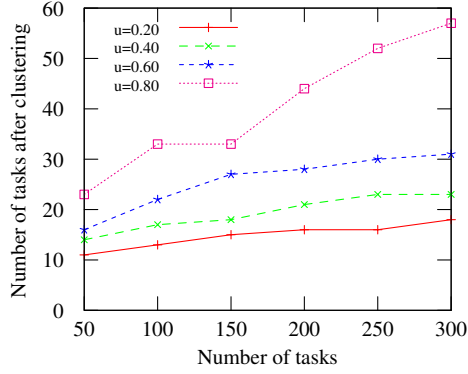
- U_i : each task utilization ($\frac{C_i}{T_i}$) is computed following the classic UUnifast [6] method. We denote as u the overall utilization factor of the processor.
- T_i : each task period is uniformly distributed between a set of 10 coprime periods. We observed that in industrial real-time embedded systems, the number of different tasks periods is usually limited (most often less than 10).
- $C_i = T_i \times U_i$
- $D_i = \text{round}((T_i - C_i) \times \text{rand}(d1, d2)) + C_i$ with $0 \leq d1 \leq d2$. This computation comes from [12] and use the following functions: $\text{rand}(d1, d2)$ which returns a pseudo-random real number uniformly distributed in the interval $[d1, d2]$ and $\text{round}(x)$ which returns the closest integer to x . We notice that $d1 = d2 = 1$ corresponds to implicit deadlines and $d1 \leq d2 = 1$ to constrained deadlines.

5.2 Results

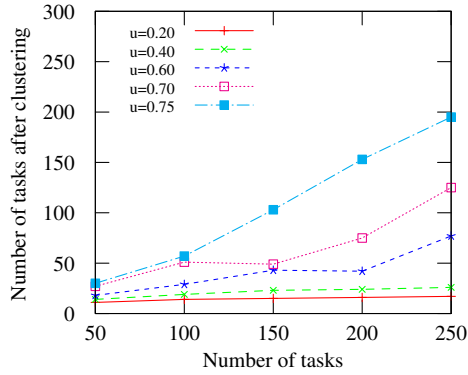
Unfortunately, as mentioned in Section 4.2, we cannot compare our heuristic with an optimal solution because the task clustering is not achievable with an exhaustive search among all partitions. Instead, we study how our heuristic behaves with various task set parameters (for example, deadline bounds).

We have implemented the heuristic in Scala [19]. Task sets range from 50 to 300 tasks by step of 50 tasks. Maximum utilization factor is fixed at 0.80 for DM and at 0.75 for EDF. Indeed, our tests show that there are only few schedulable task sets (according to the tests used) generated above those values. We only take into account task sets that are initially schedulable. We compute average results by executing several times the heuristic on randomly generated task sets with the same parameters.

We observe in Figure 4(a) that the technique is efficient under DM. Indeed, the number of tasks obtained after clustering is approximately linear in the number of tasks



(a) Task clustering under DM.



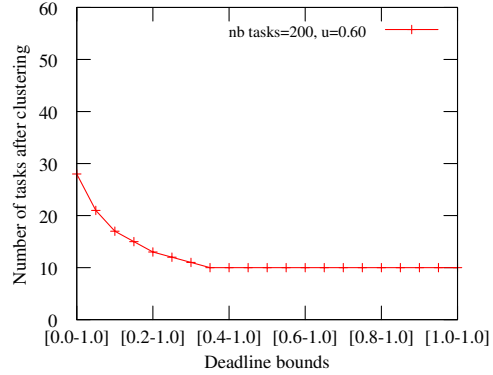
(b) Task clustering under EDF.

Figure 4: Results of task clustering.

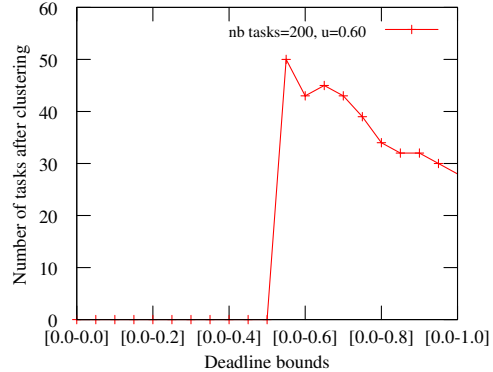
and the slope of the curve is rather limited. However, results under EDF test in Figure 4(b) are not as satisfying. Clustering is less efficient, especially when the utilization goes over 0.6. This difference probably comes from the fact that the clustering affects more the test under EDF than the test under DM. Finally notice that, the higher the utilization factor is, the less the tasks are clustered.

Figure 5(a) and Figure 5(b) present the clustering depending on deadline bound variations with DM. For instance, $[0.4 - 1.0]$ on the horizontal axis means that the deadline is chosen between 40% and 100% of the period minus the execution time. We can see in Figure 5(a) that the number of clusters is minimal (equal to the number of different periods) when the deadline lower bound is

about 40% of the period minus the execution time. Figure 5(b) shows that no clustering is possible before the upper bound gets to around 60%. Above that bound, the efficiency of the clustering improves steadily (the number of clusters decreases).



(a) Variation of deadline lower bound.

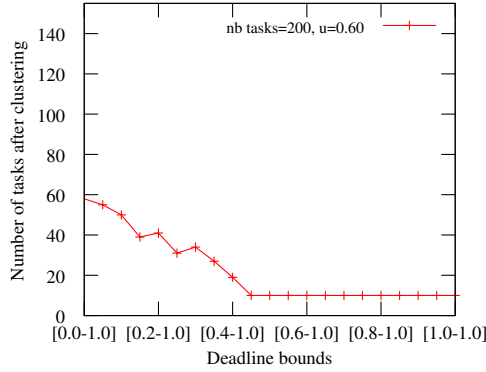


(b) Variation of deadline upper bound.

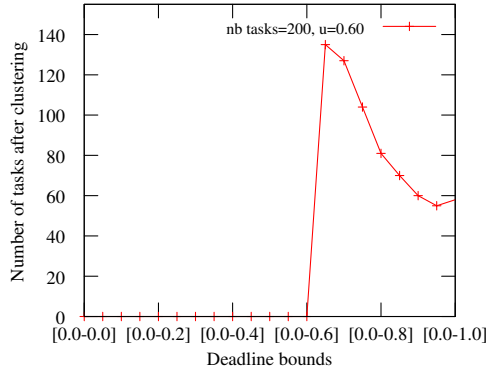
Figure 5: Task clustering with DM: impact of deadline bounds.

Figure 6(a) and Figure 6(b) present the clustering for the same deadline variations with EDF. The overall trends of the curves are similar, though the clustering is overall less efficient.

These results show that the deadline bounds have the most significant impact on the clustering (even more than the number of tasks for DM). Both with DM and EDF, the clustering is the most efficient with deadlines bounds



(a) Variation of deadline lower bound.



(b) Variation of deadline upper bound.

Figure 6: Task clustering with EDF: impact of deadline bounds.

in the interval $[0.5, 1]$. Indeed, the closer deadlines are to the period, the more margin is left for the clustering. The clustering is even maximal in that interval because we get as many tasks as the number of different periods, both for DM and EDF. Notice that according to further experiments, this remains true for a higher number of distinct periods.

6 Conclusion and future work

We proposed a heuristic to automatically reduce a large set of independent tasks to a smaller set, while preserving the schedulability of the task set. The current assumption

that tasks are independent will be lifted in future work. The present work is meant to lay the foundations of automated task clustering, which, as far as we know, has not been studied formally before.

Experimental results point out that under some ranges of deadline bounds, the clusterings are maximal (i.e. the number of tasks equals the number of periods). As these ranges are actually realistic, it would be interesting to try to formally prove that we can always reach maximal clusterings for these bounds. Such a property would allow to directly gather all the tasks with the same periods without using any clustering algorithm.

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